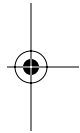
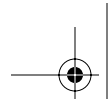


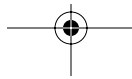
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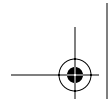




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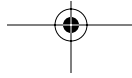


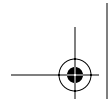
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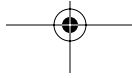
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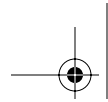
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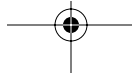
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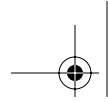
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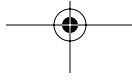
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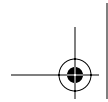
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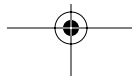
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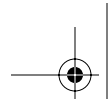
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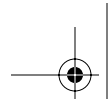
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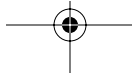
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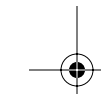
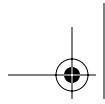
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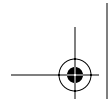
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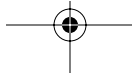
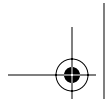


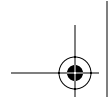


# Preface

S.T. Rachev's research was supported by grants from Division of Mathematical, Life and Physical Sciences, College of Letters and Science, University of California, Santa Barbara and the Deutschen Forschungsgemeinschaft.







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Christian Menn  
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